

Deep Generative Models



UNIVERSITÀ
DEGLI STUDI
DI MILANO



IWR Summer School | **Heidelberg**
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- Check LivingReview for many **ML4HEP applications**



Plan of attack



1. Basics of DGMs and Normalizing Flows
2. GANs, VAE and SurVAE
3. Diffusion Models

Blackboard Session I

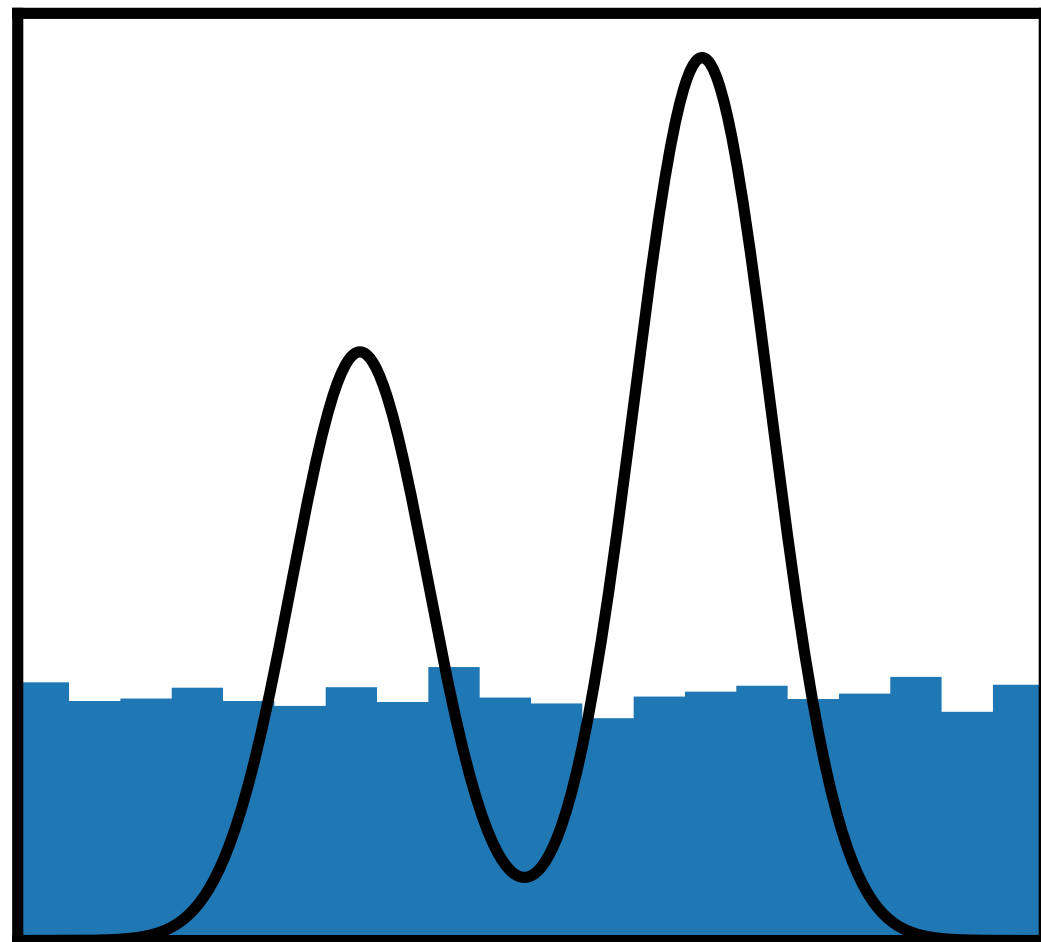
Normalizing Flows

Neural Importance Sampling

Monte Carlo integration

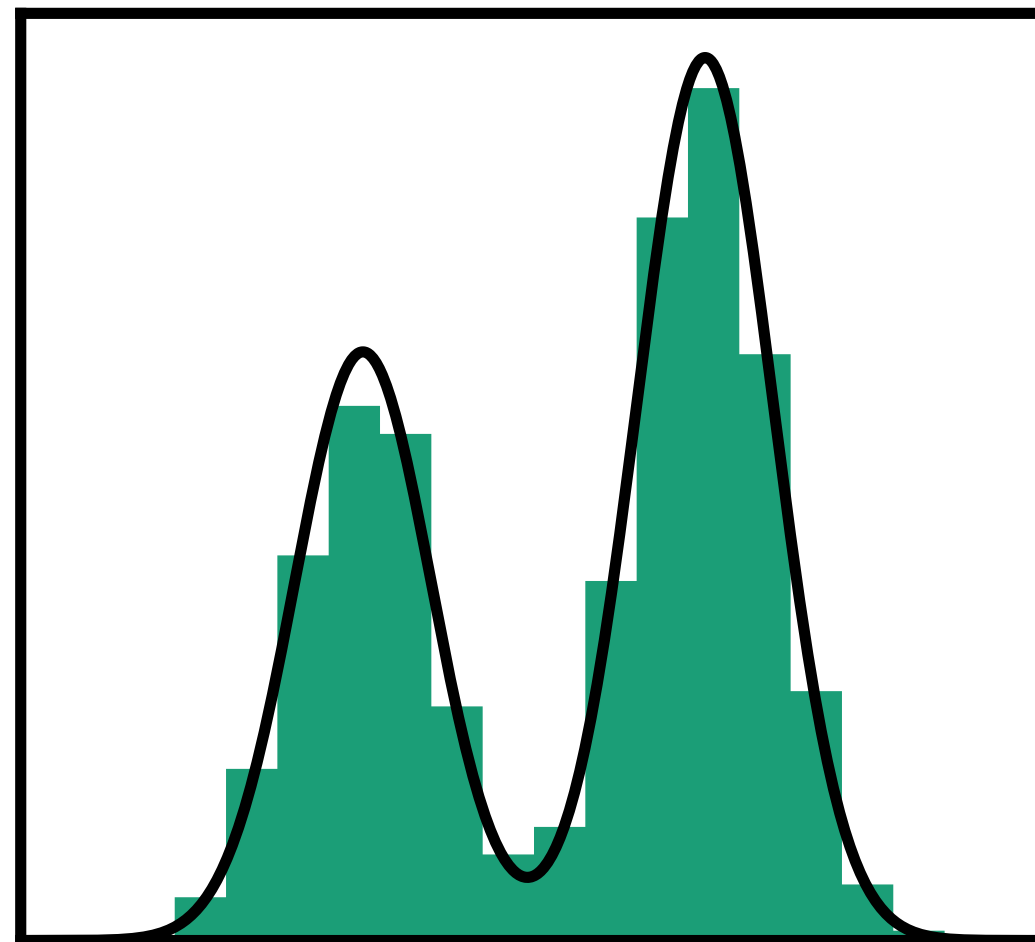
Calculate (differential) cross sections

$$d\sigma = \frac{1}{\text{flux}} dx_a dx_b f(x_a) f(x_b) d\Phi_n \langle |M_{\lambda,c,\dots}(p_a, p_b | p_1, \dots, p_n)|^2 \rangle$$



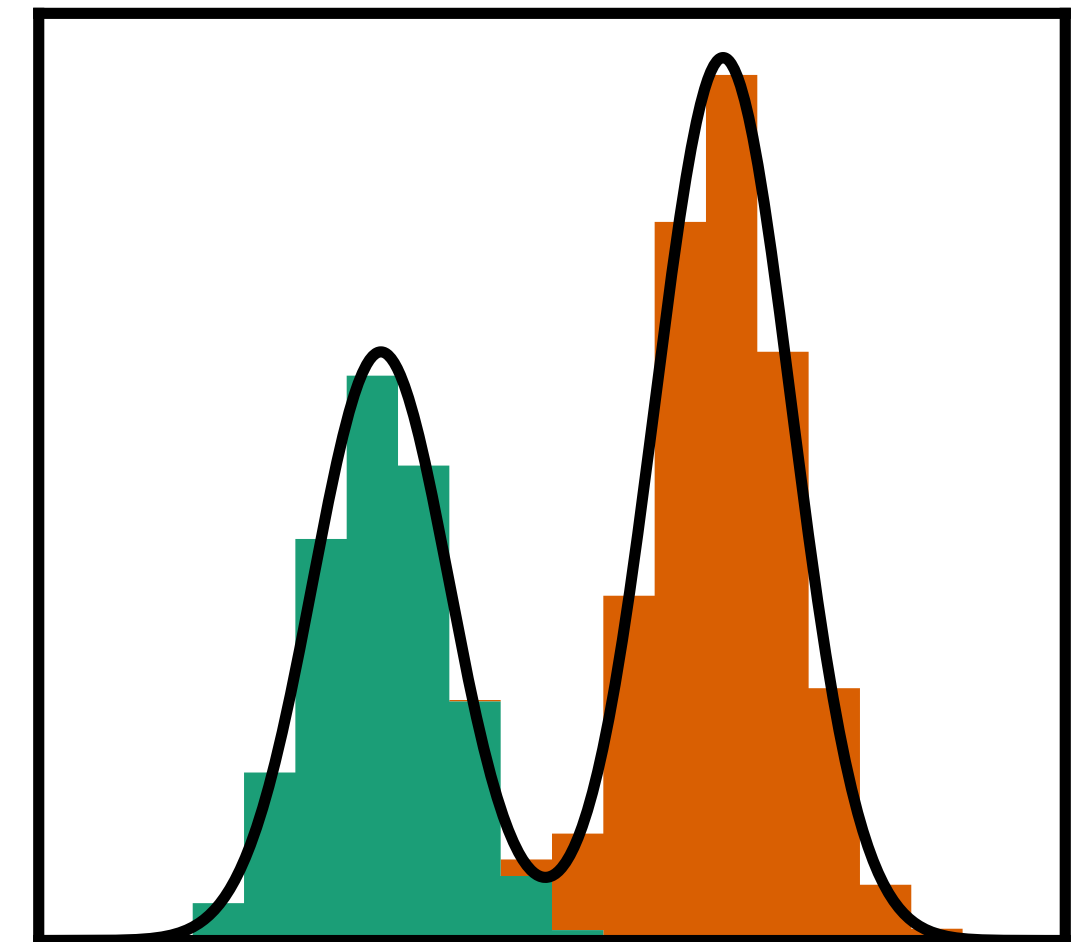
Flat sampling:
inefficient

$$I = \langle f(x) \rangle_{x \sim \text{unif}}$$



Importance sampling:
find p close to f

$$I = \left\langle \frac{f(x)}{p(x)} \right\rangle_{x \sim p(x)}$$



Multi-channel:
one map for each channel

$$I = \sum_i \left\langle \alpha_i(x) \frac{f(x)}{p_i(x)} \right\rangle_{x \sim p_i(x)}$$

Event generation in MadGraph



Calculate (differential) cross sections

$$d\sigma = \frac{1}{\text{flux}} dx_a dx_b f(x_a) f(x_b) d\Phi_n \left\langle |M_{\lambda,c,\dots}(p_a, p_b | p_1, \dots, p_n)|^2 \right\rangle$$



Sum over channels

MadGraph: build channels from Feynman diagrams

Integrand

MadGraph: $d\sigma/dx$

$$I = \sum_i \left\langle \alpha_i(x) \frac{f(x)}{p_i(x)} \right\rangle_{x \sim p_i(x)}$$

Channel weights

MadGraph: $\alpha_i^{\text{MG}}(x) \sim |M_i|^2$

Channel mappings

MadGraph: use amplitude structure, ...
Analytic mappings + refine with **VEGAS**
(factorized, histogram based importance sampling)

Event generation in MadNIS



Calculate (differential) cross sections

$$d\sigma = \frac{1}{\text{flux}} dx_a dx_b f(x_a) f(x_b) d\Phi_n \left\langle |M_{\lambda,c,\dots}(p_a, p_b | p_1, \dots, p_n)|^2 \right\rangle$$



Sum over channels

MadGraph: build channels
from Feynman diagrams

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MadGraph: $d\sigma/dx$

Channel weights

MadGraph: $\alpha_i^{\text{MG}}(x) \sim |M_i|^2$

$$I = \sum_i \left\langle \alpha_i(x) \frac{f(x)}{p_i^\omega(x)} \right\rangle_{x \sim p_i^\omega(x)}$$

Learned channel mappings

MadGraph: use amplitude structure, ...
Analytic mappings + refine with ~~VEGAS~~

refine with **NF**

Event generation in MadNIS



Calculate (differential) cross sections

$$d\sigma = \frac{1}{\text{flux}} dx_a dx_b f(x_a) f(x_b) d\Phi_n \langle |M_{\lambda,c,\dots}(p_a, p_b | p_1, \dots, p_n)|^2 \rangle$$



Sum over channels

MadGraph: build channels
from Feynman diagrams

Integrand

MadGraph: $d\sigma/dx$

$$I = \sum_i \left\langle \alpha_i^\xi(x) \frac{f(x)}{p_i^\omega(x)} \right\rangle_{x \sim p_i^\omega(x)}$$

Learned channel weights

MadGraph: $\alpha_i^{\text{MG}}(x) \sim |M_i|^2$

$$\alpha_i(x) \rightarrow \alpha_i^\xi(x) = \alpha_i^{\text{MG}}(x) \cdot K_i^\xi(x)$$

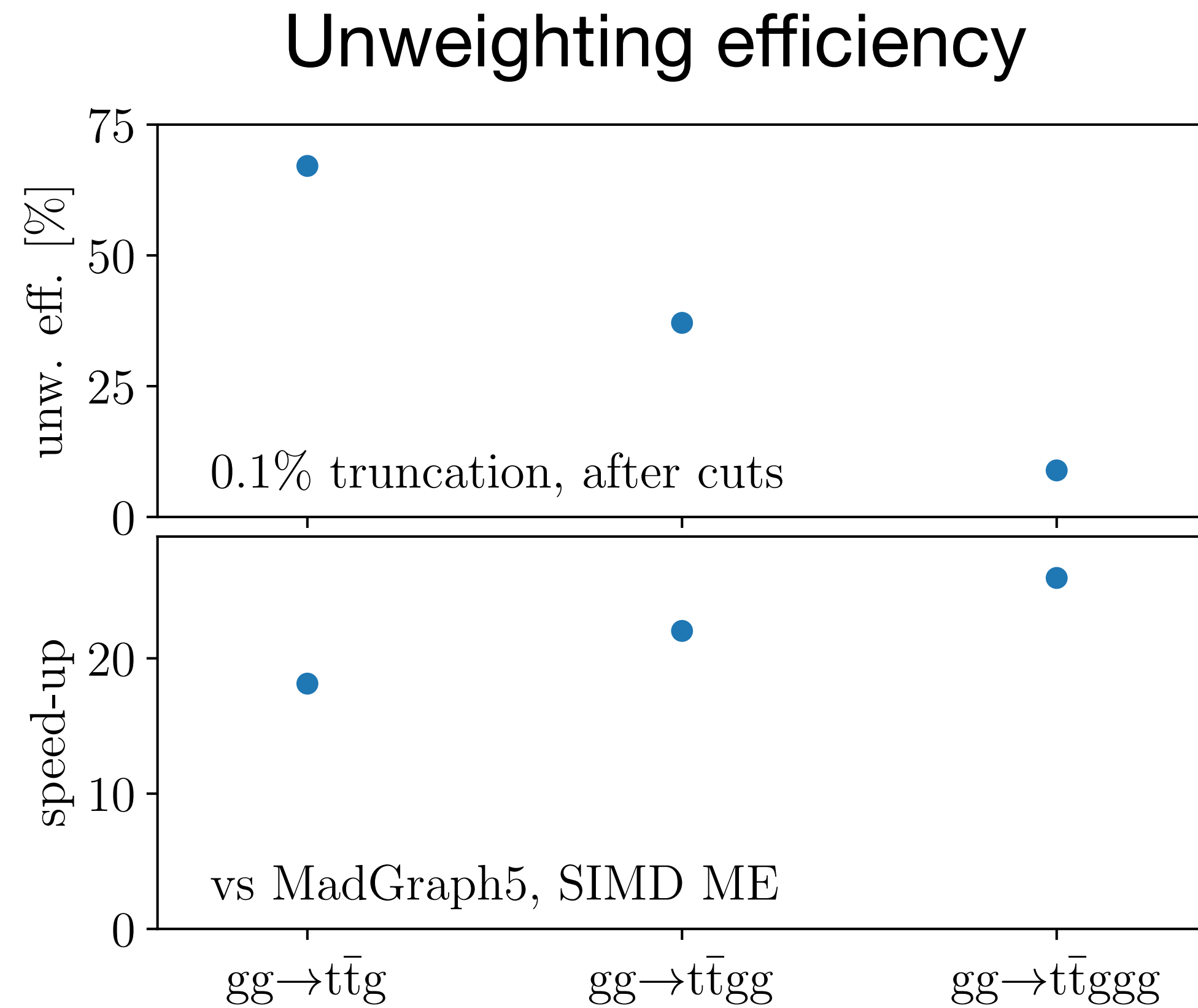
parametrize with **NN**

Learned channel mappings

MadGraph: use amplitude structure, ...
Analytic mappings + ~~refine with VEGAS~~

refine with **NF**

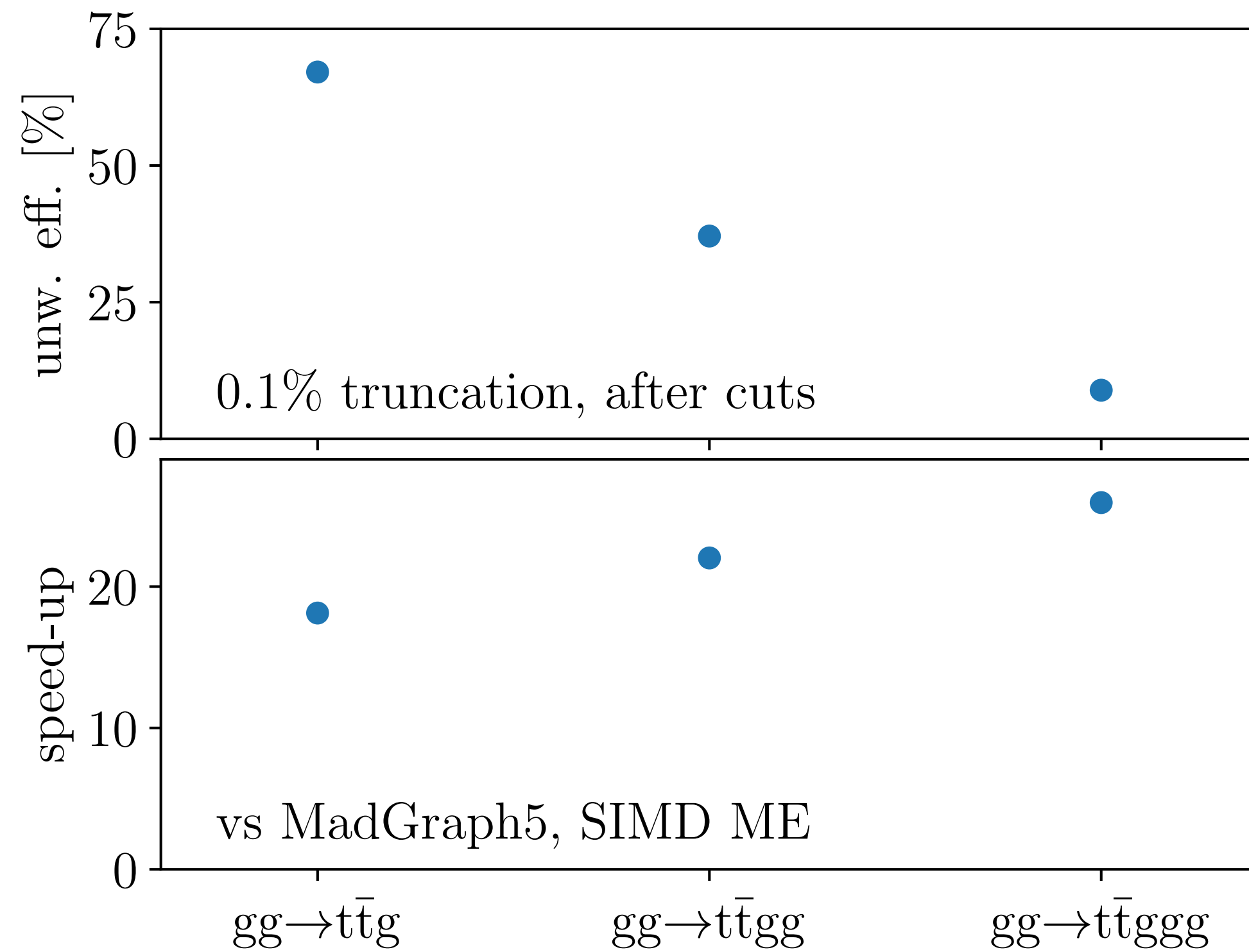
Unweighting performance



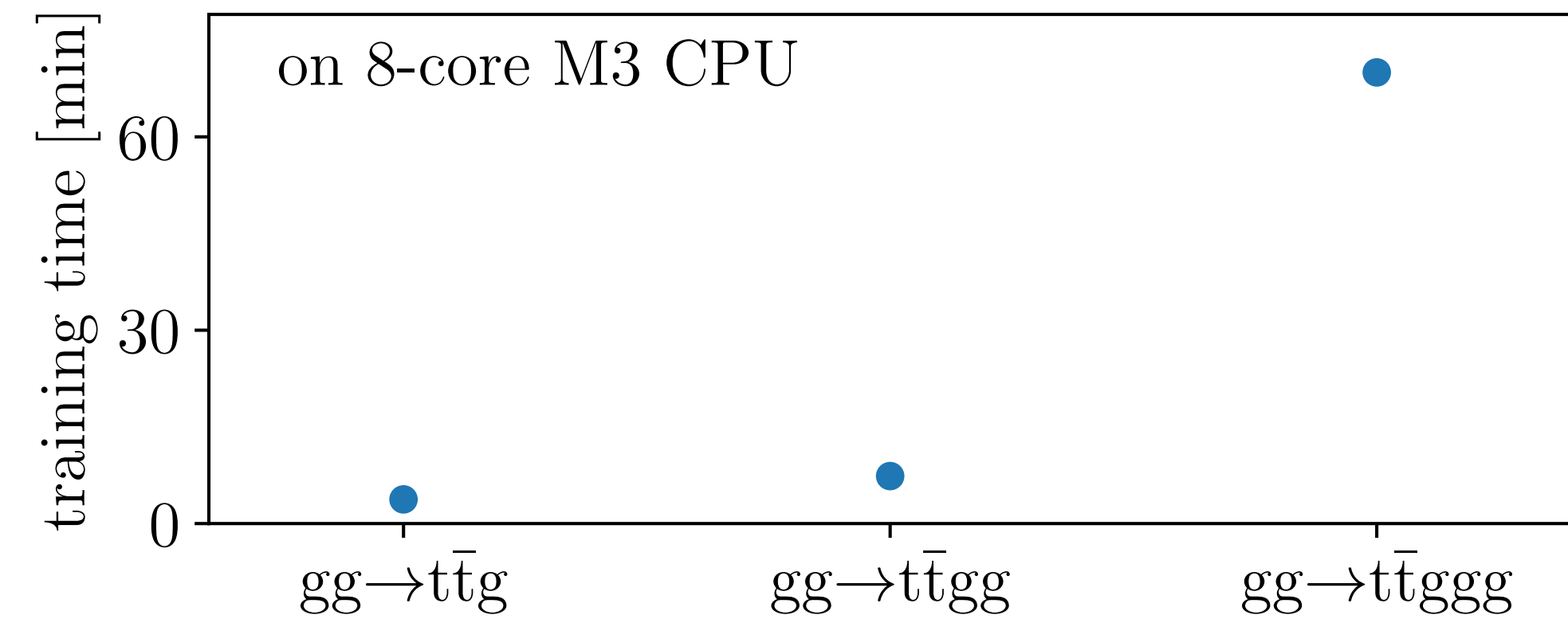
(preliminary)

Unweighting performance

Unweighting efficiency



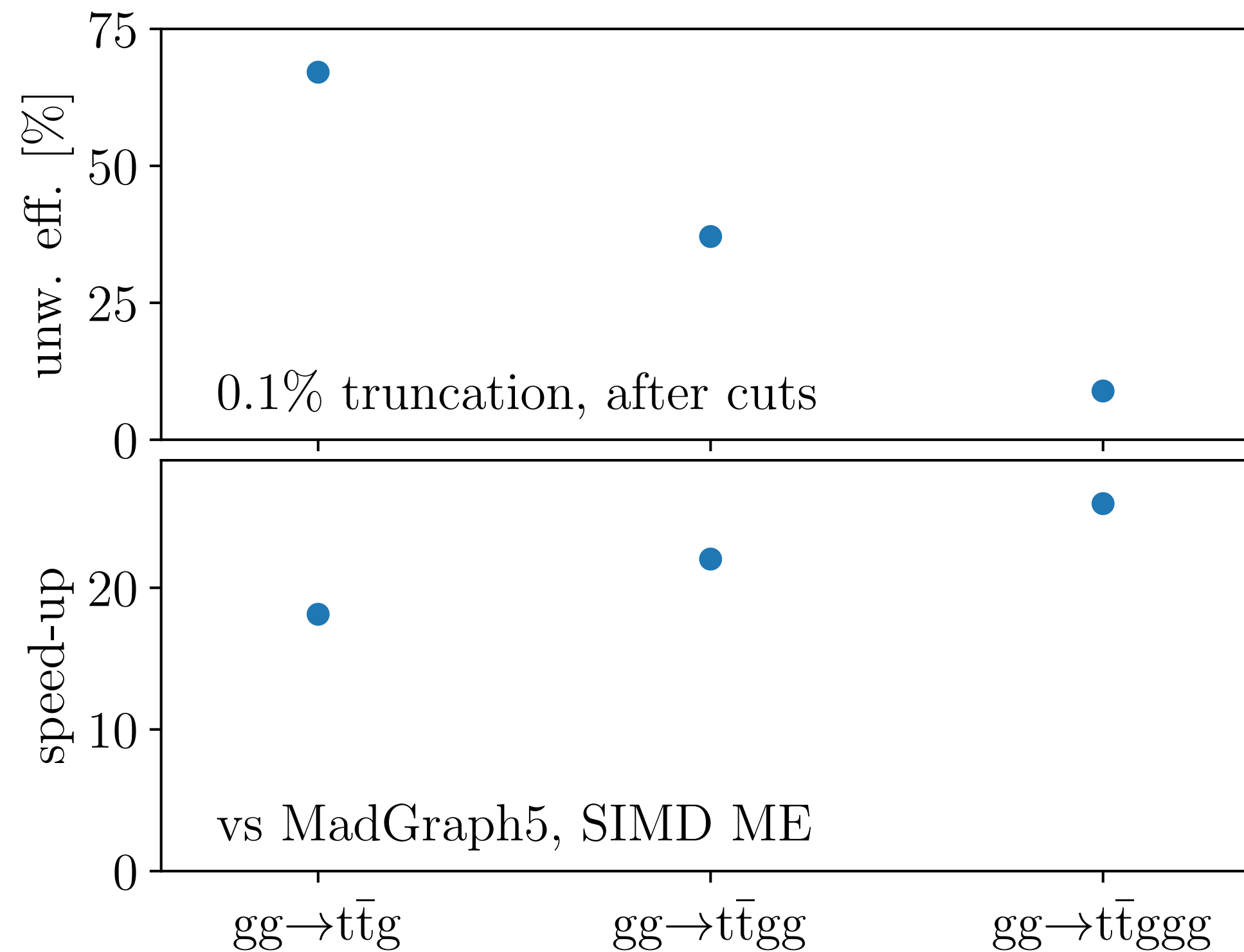
Training time



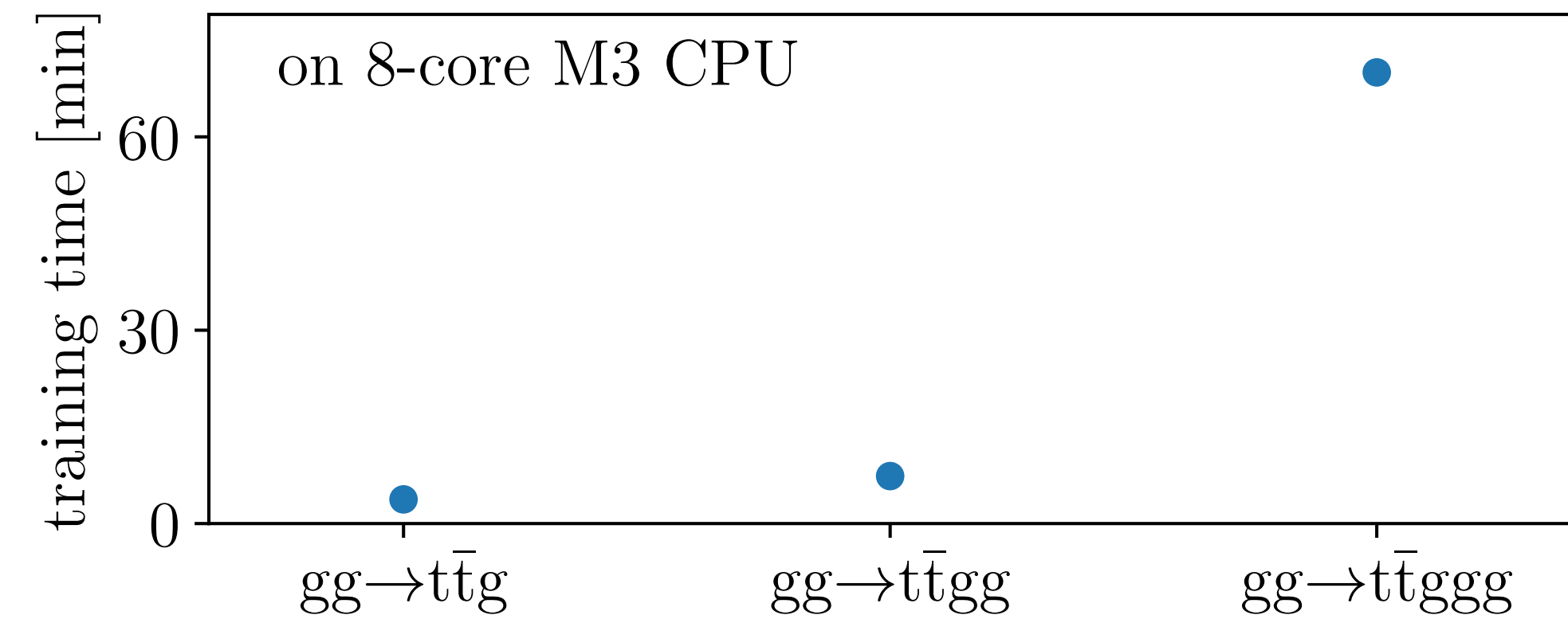
(preliminary)

Unweighting performance

Unweighting efficiency

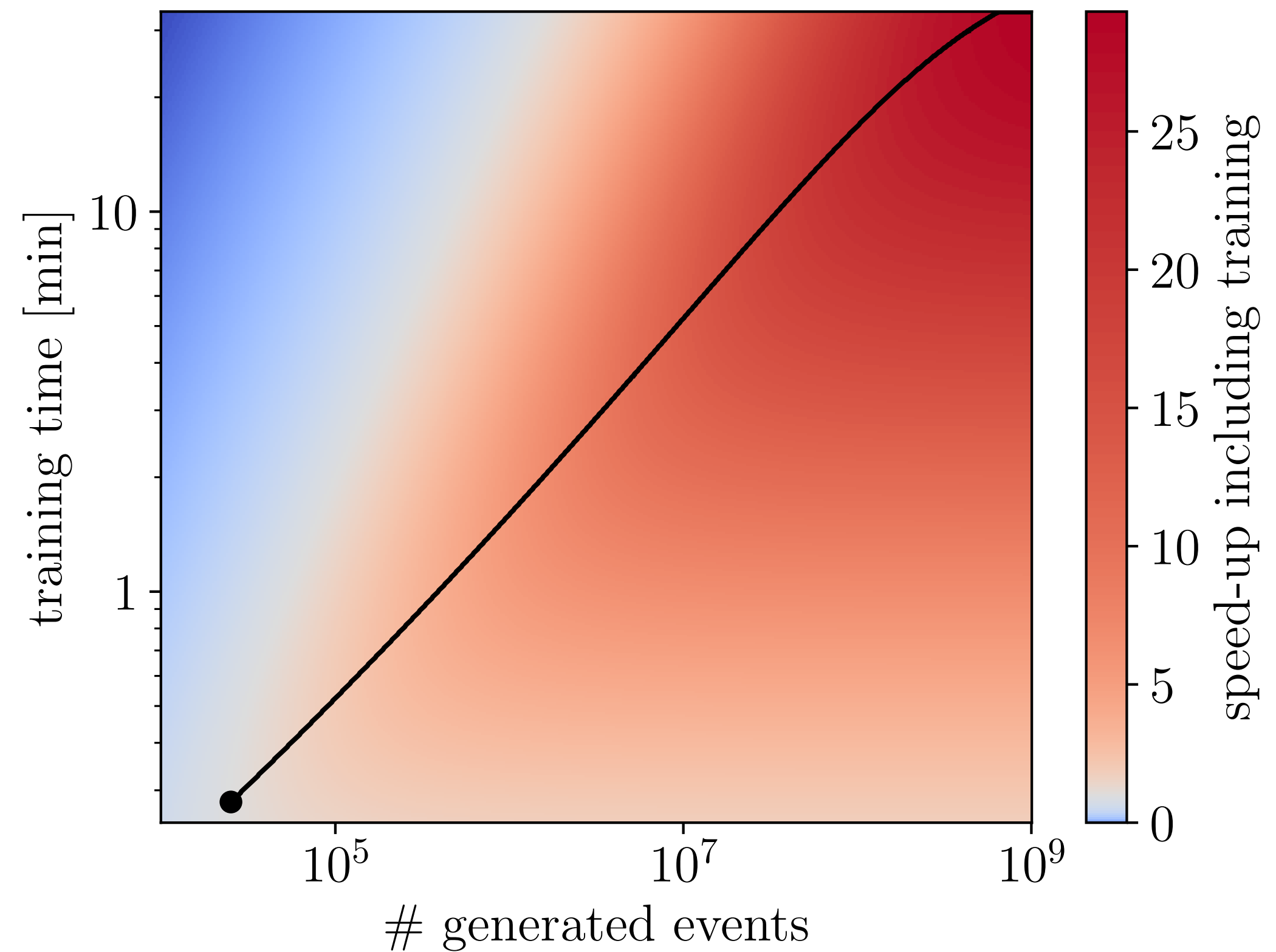
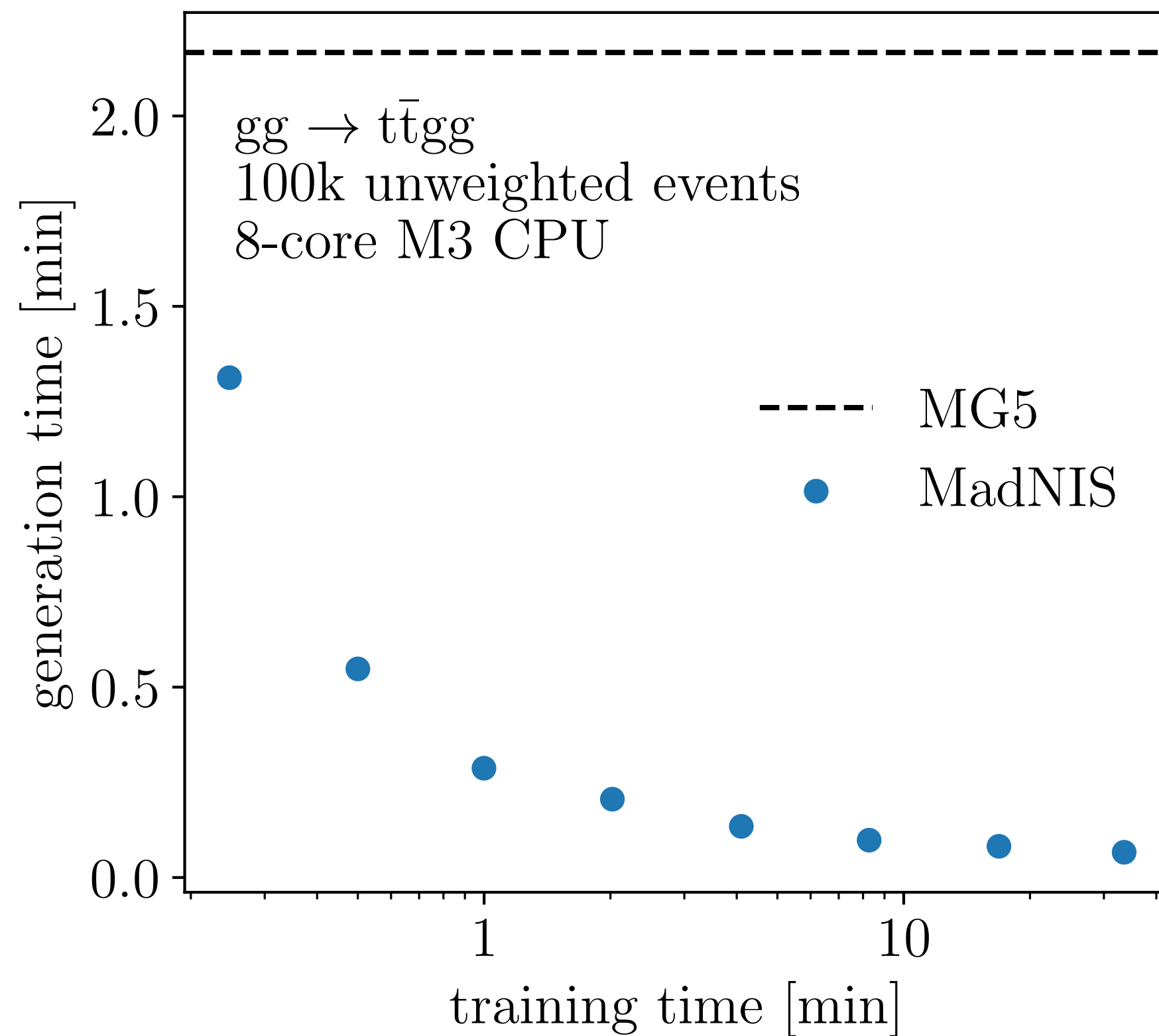


Training time



→ Does it still pay off?

Training time and amortization

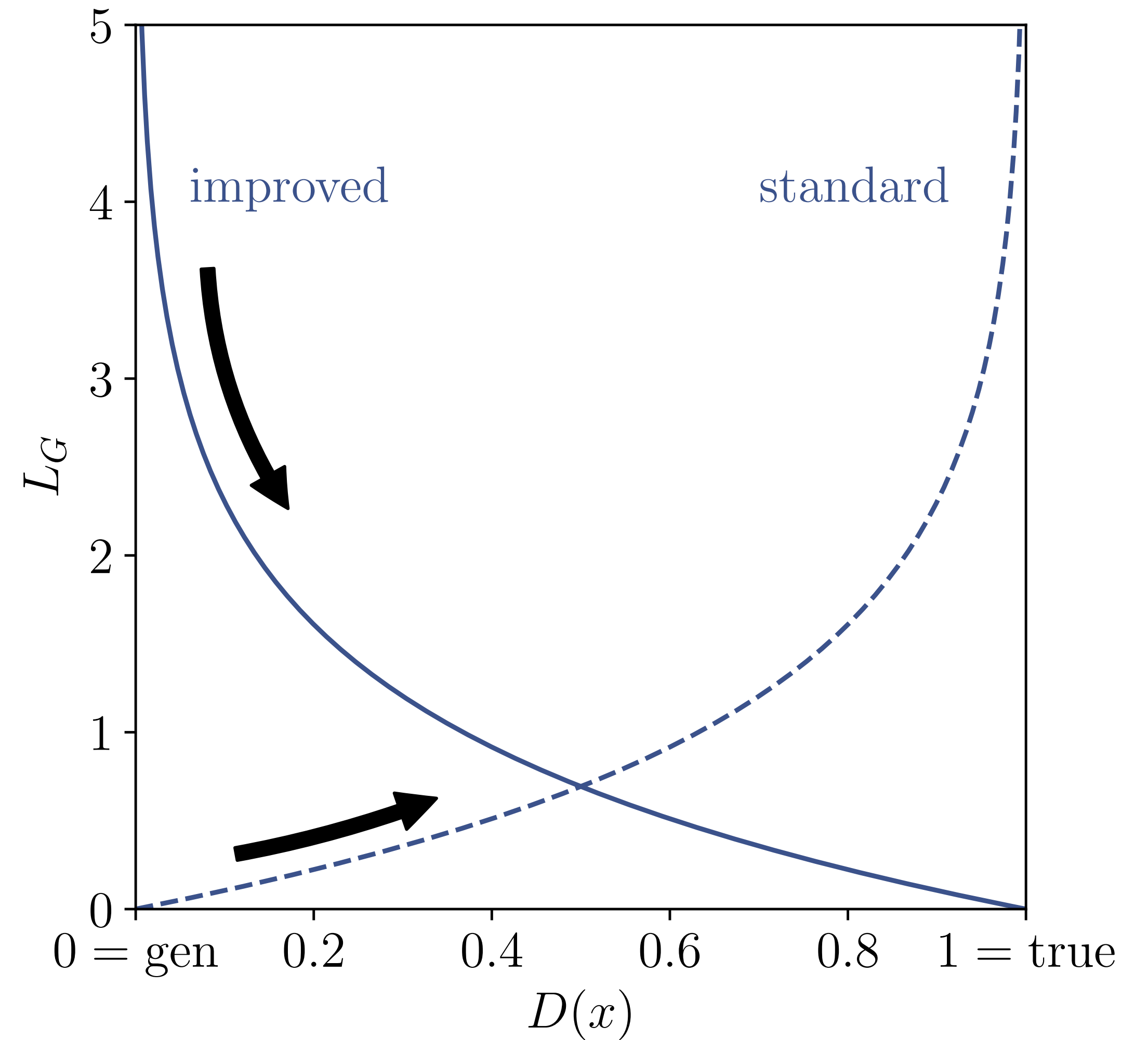
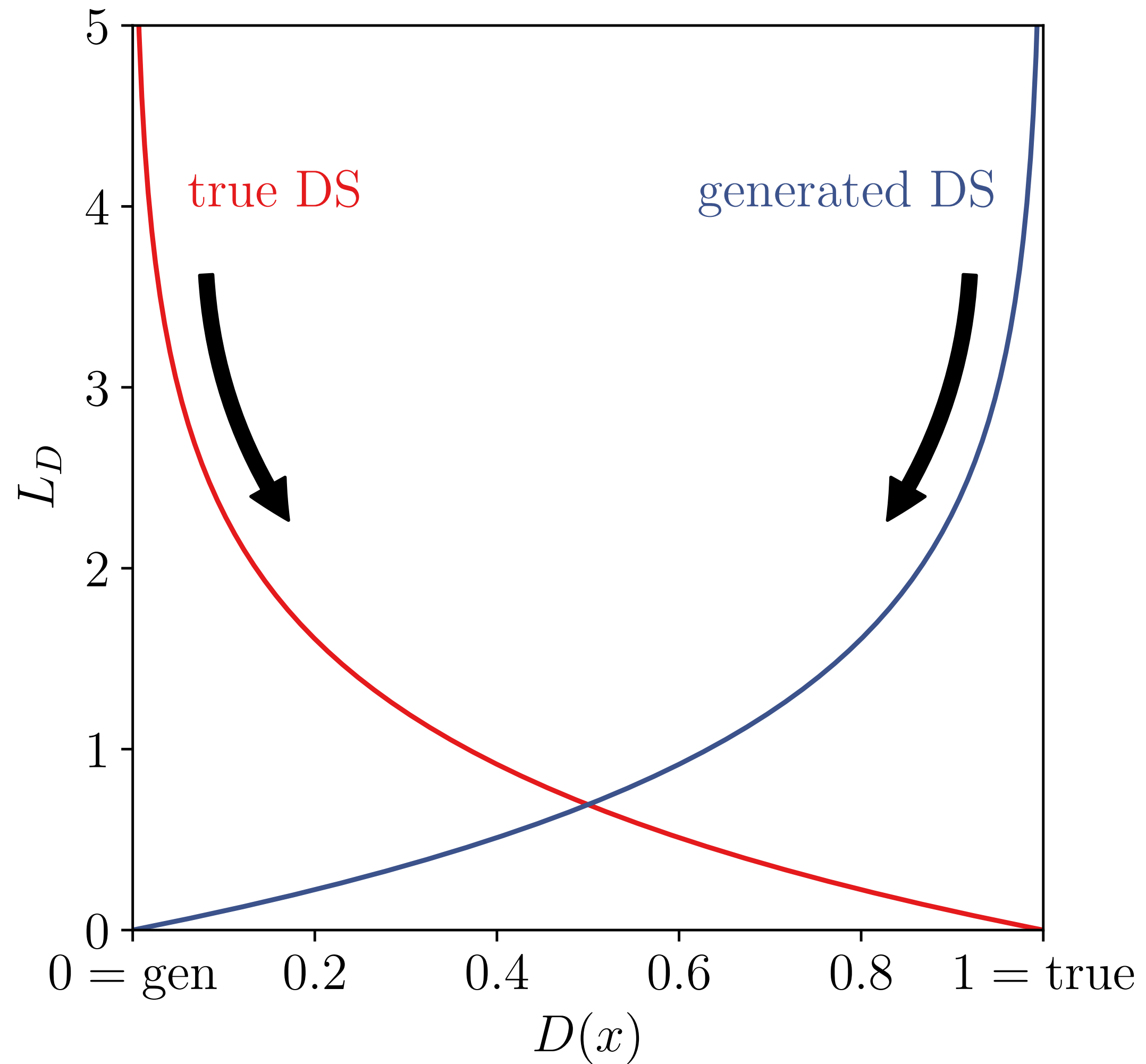


(preliminary)

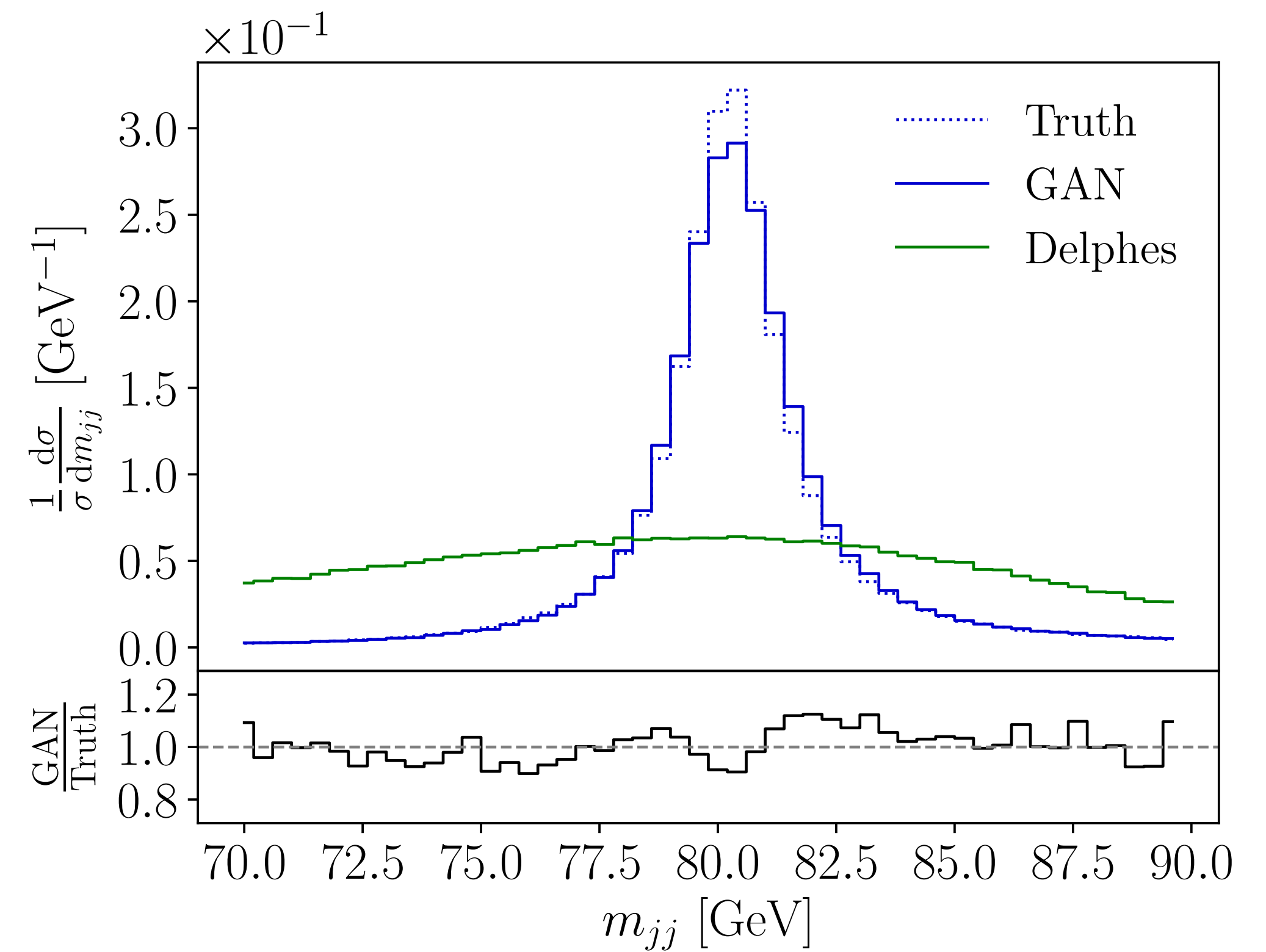
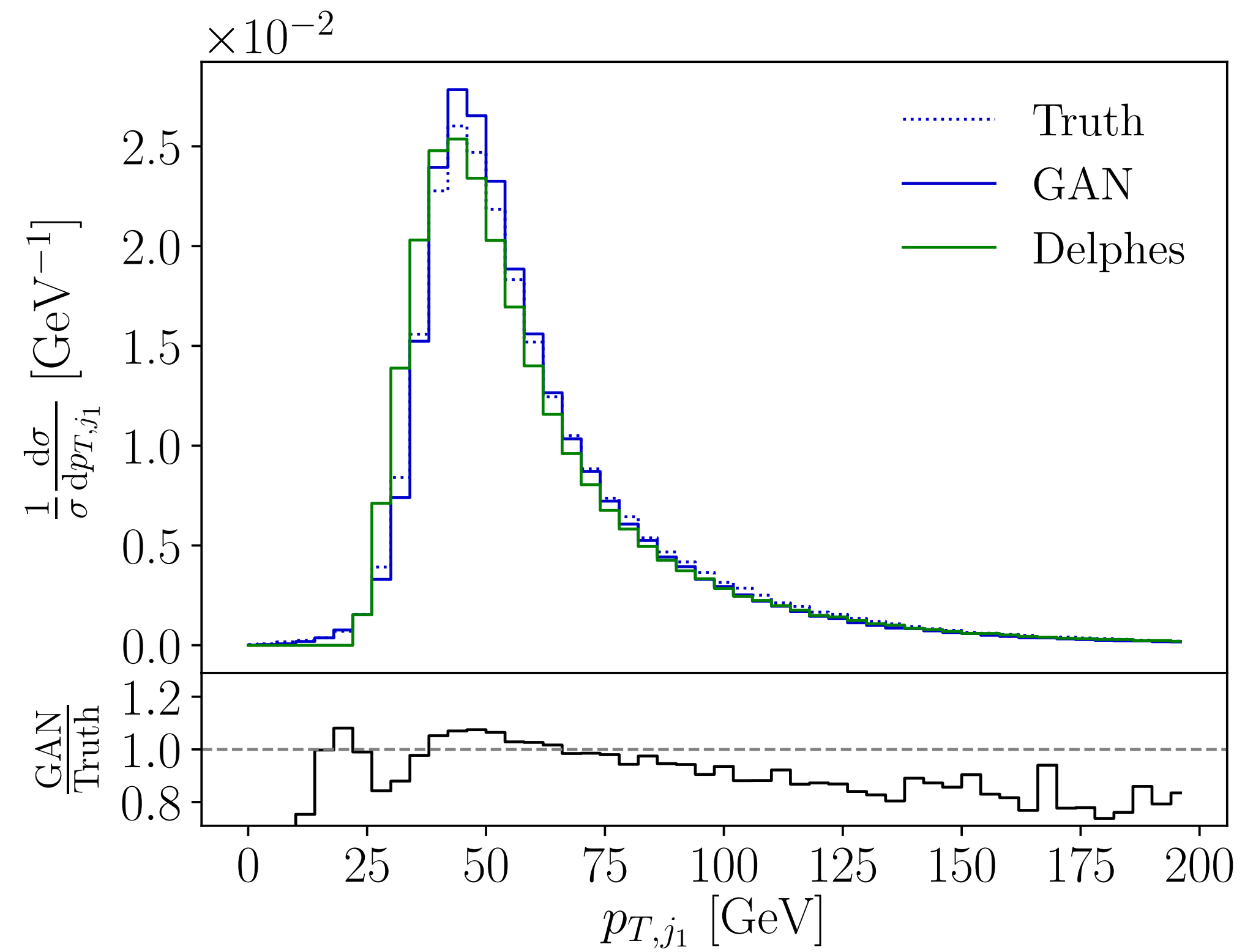
MadNIS is faster starting at 10k events!

Blackboard Session II

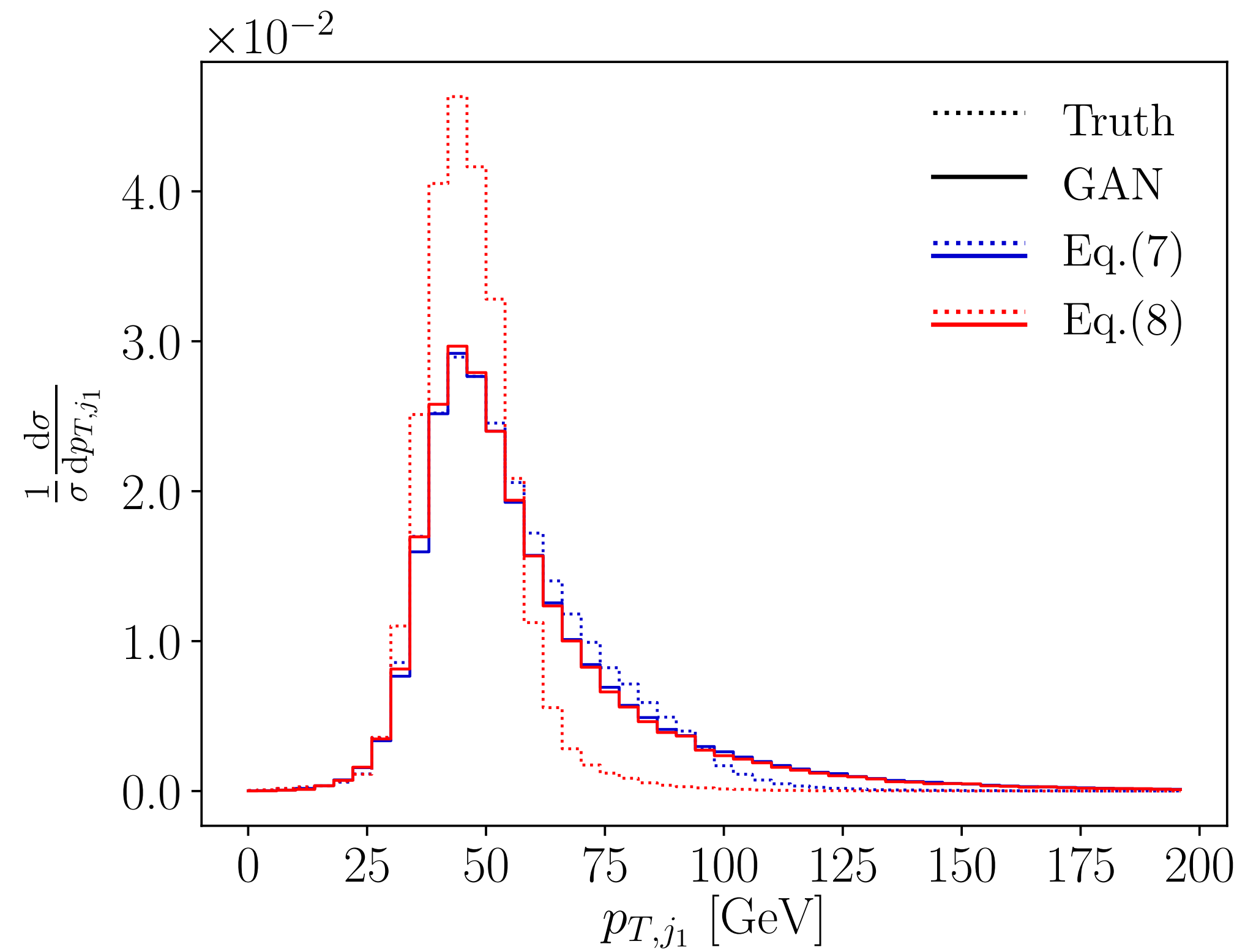
GAN Loss



GAN Unfolding



GAN Unfolding



Cut I:

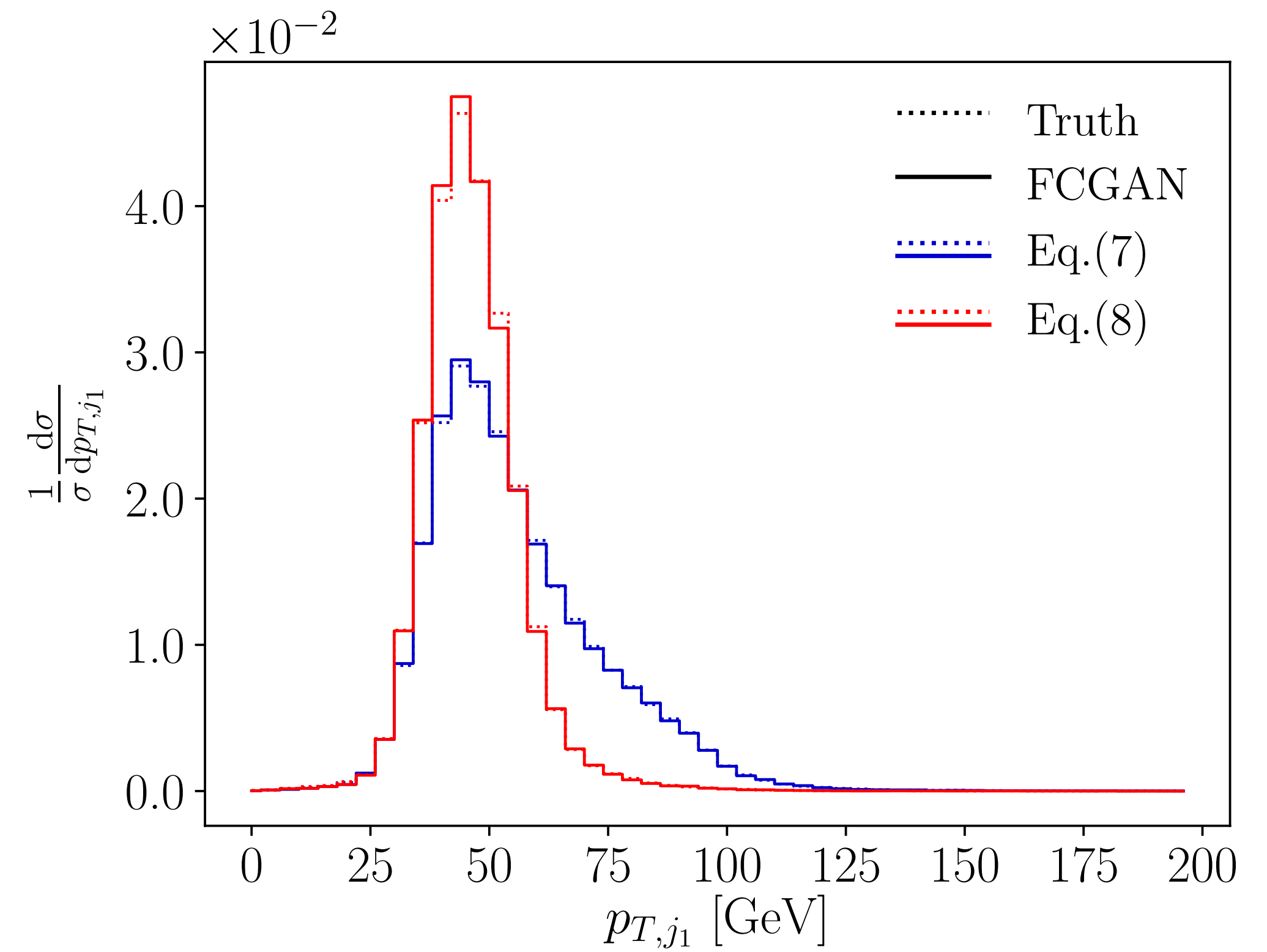
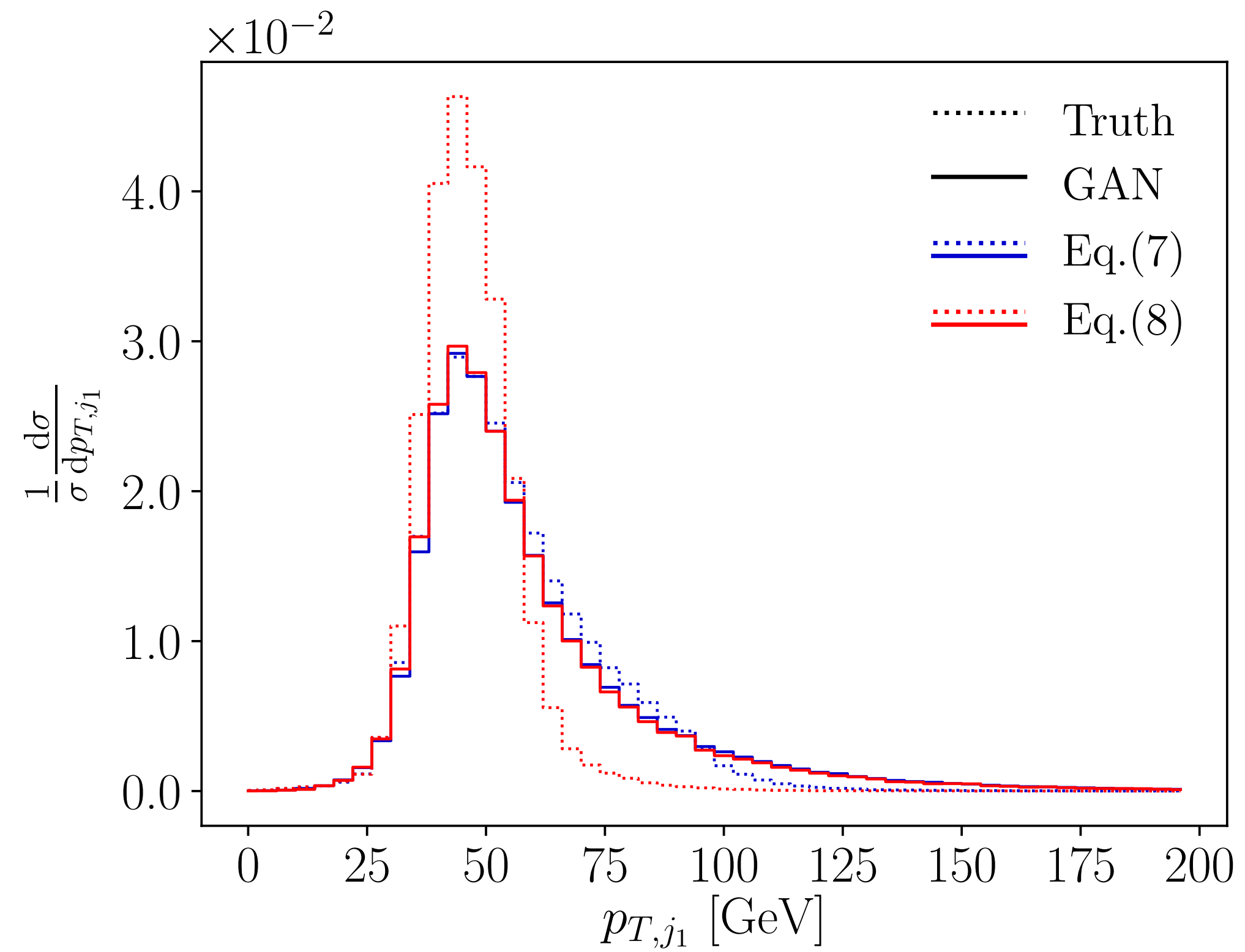
$$30 \text{ GeV} < p_{T,j1} < 100 \text{ GeV}$$

Cut II:

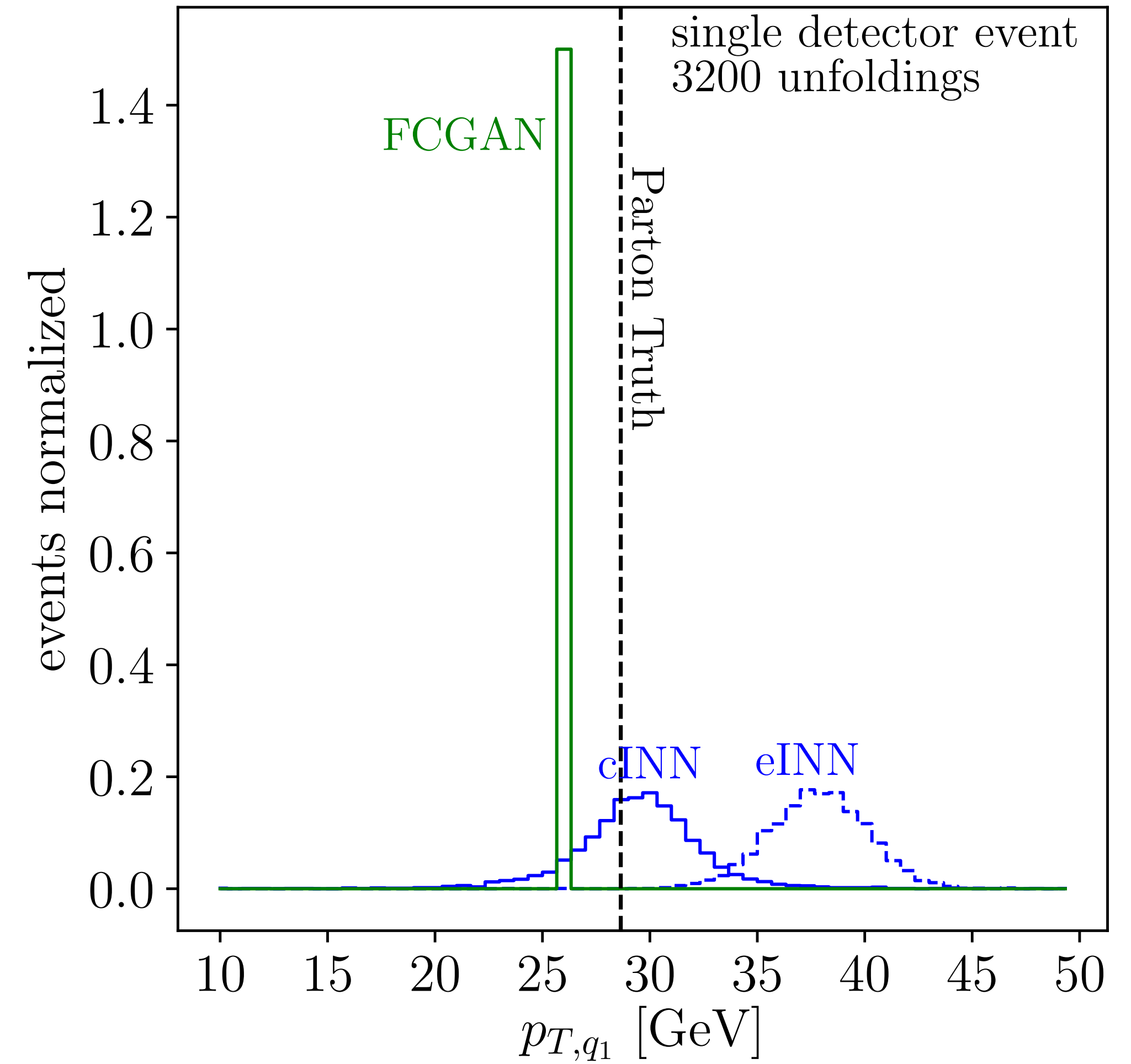
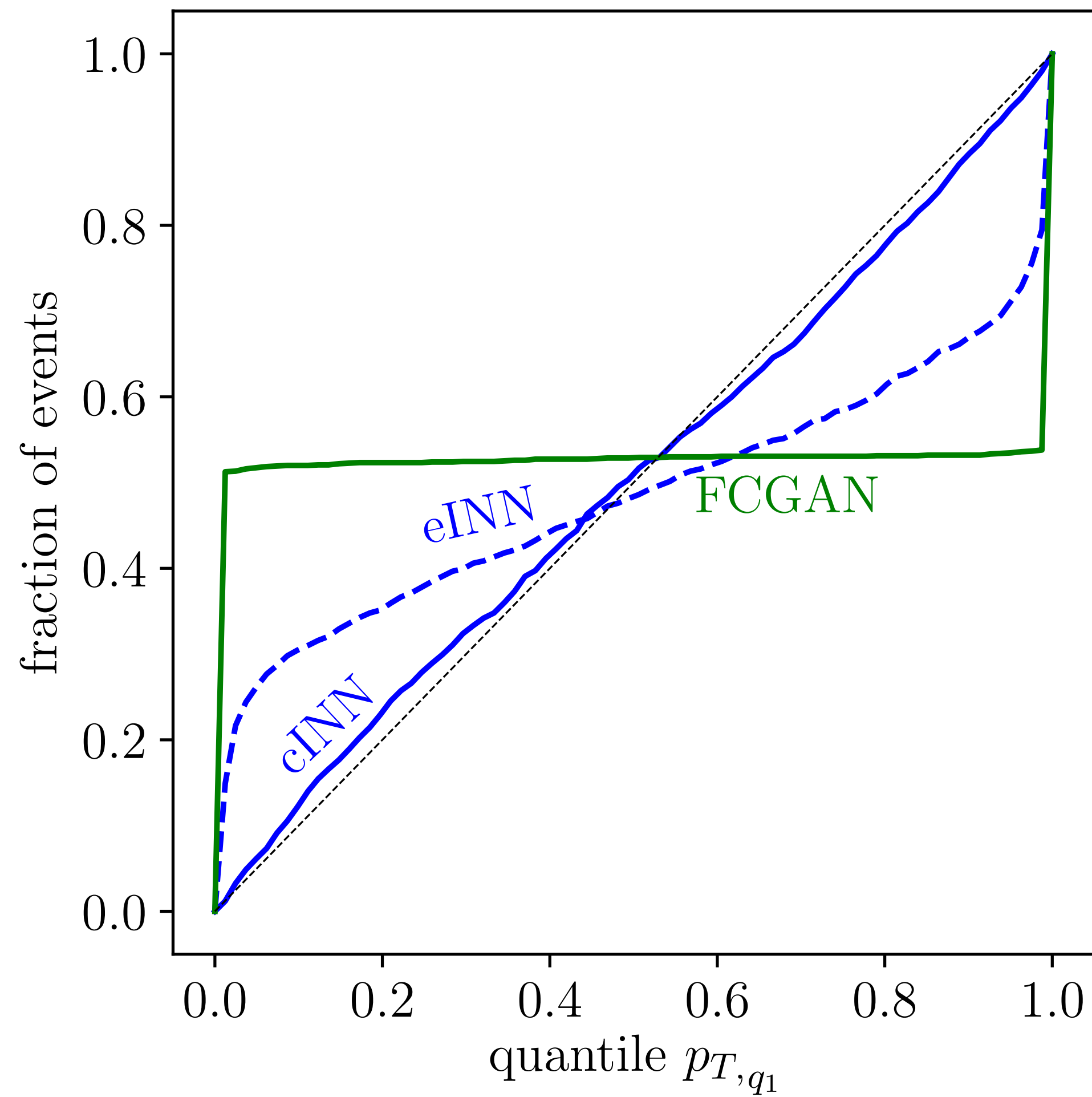
$$30 \text{ GeV} < p_{T,j1} < 50 \text{ GeV}$$

$$30 \text{ GeV} < p_{T,j2} < 60 \text{ GeV}$$

FCGAN Unfolding

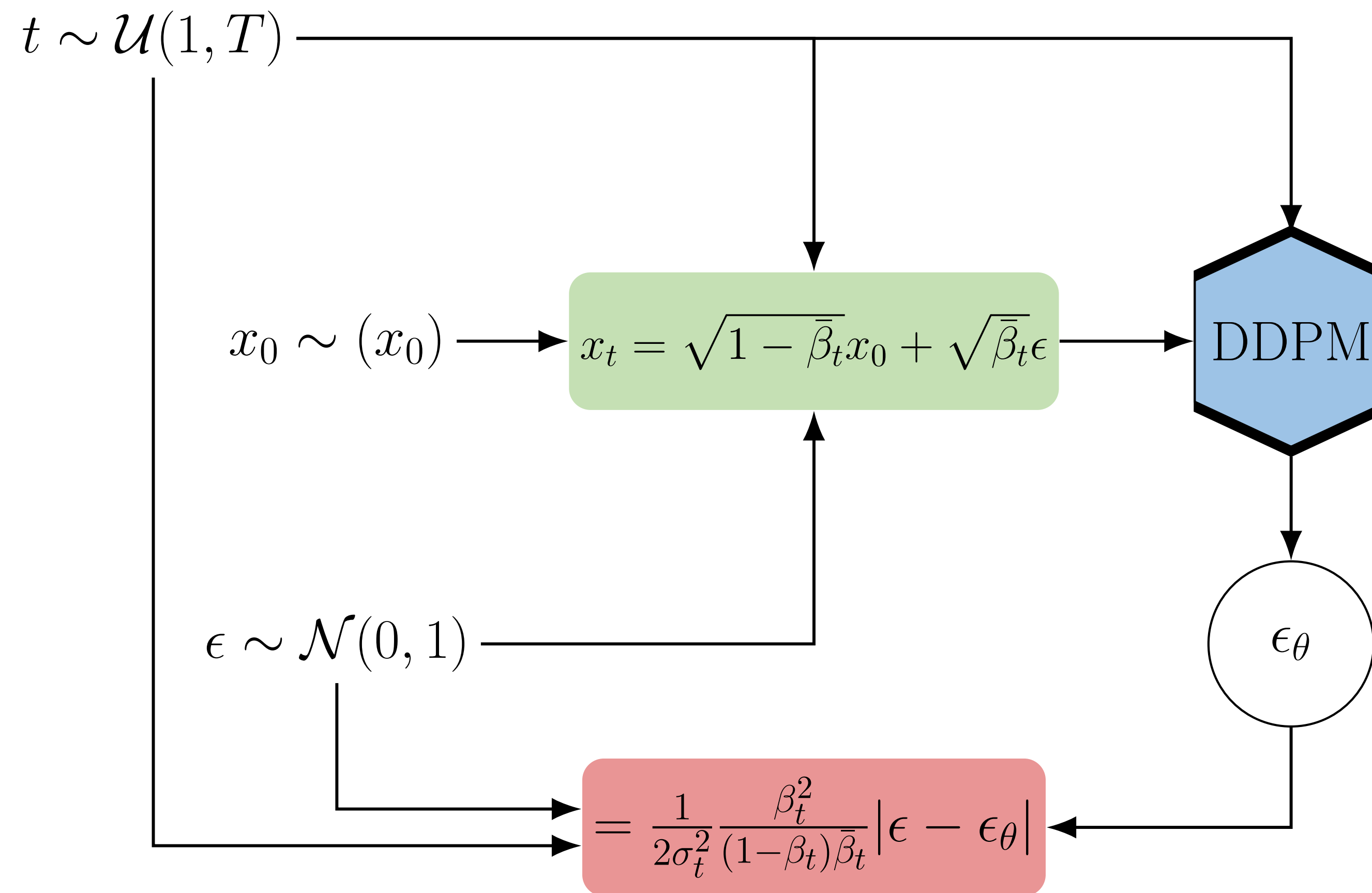


cINN Unfolding

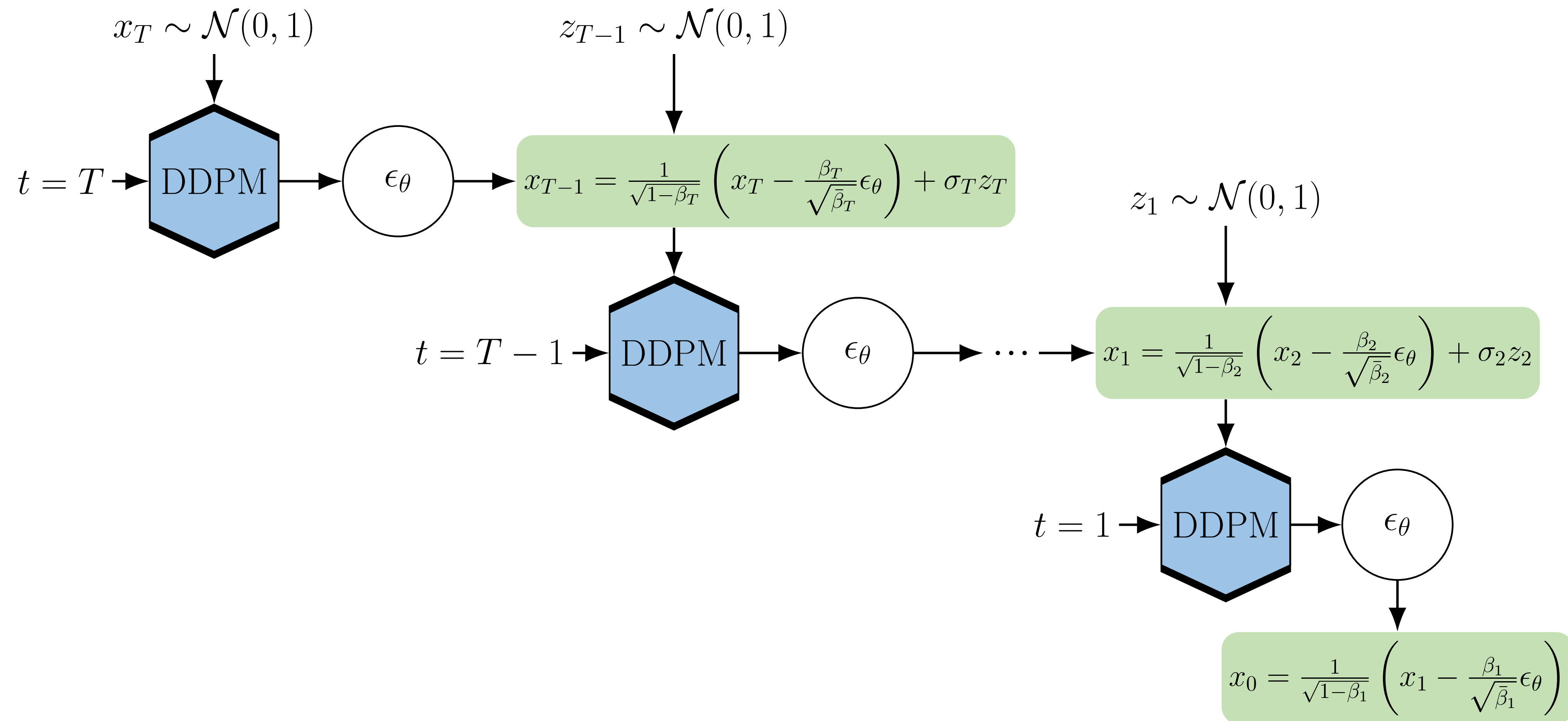


Blackboard Session III

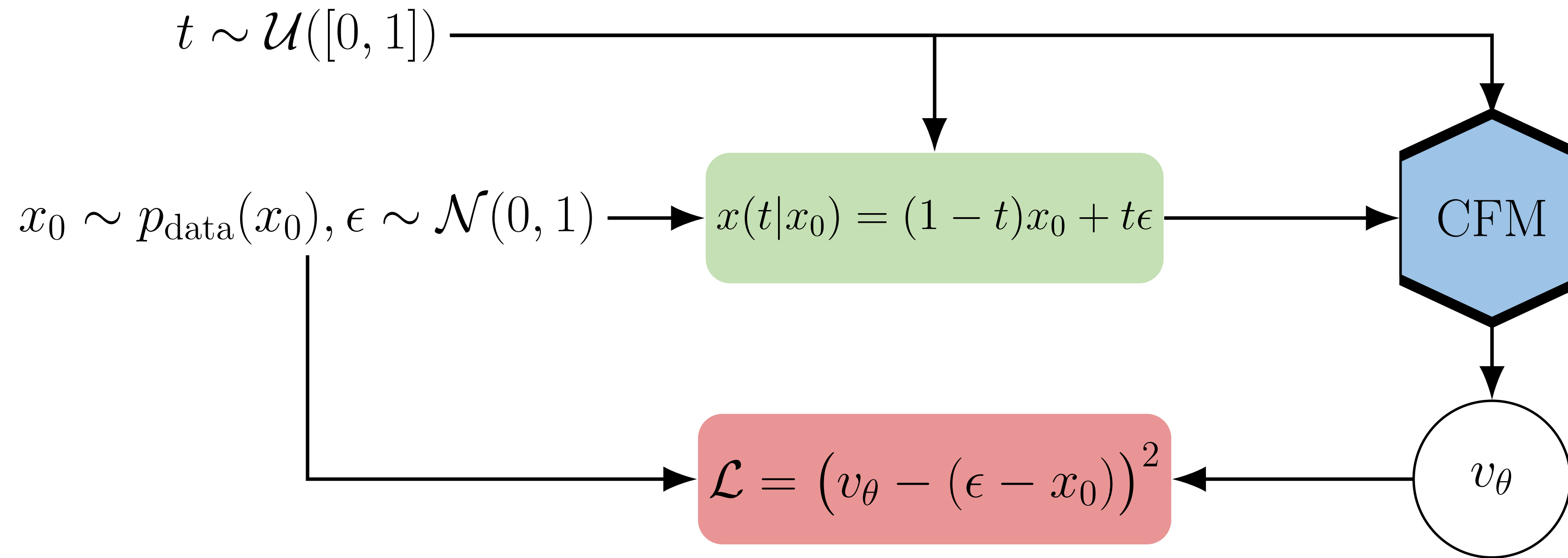
DDPM Training



DDPM Sampling



CFM Training and Sampling



Solve ODE numerically for sampling

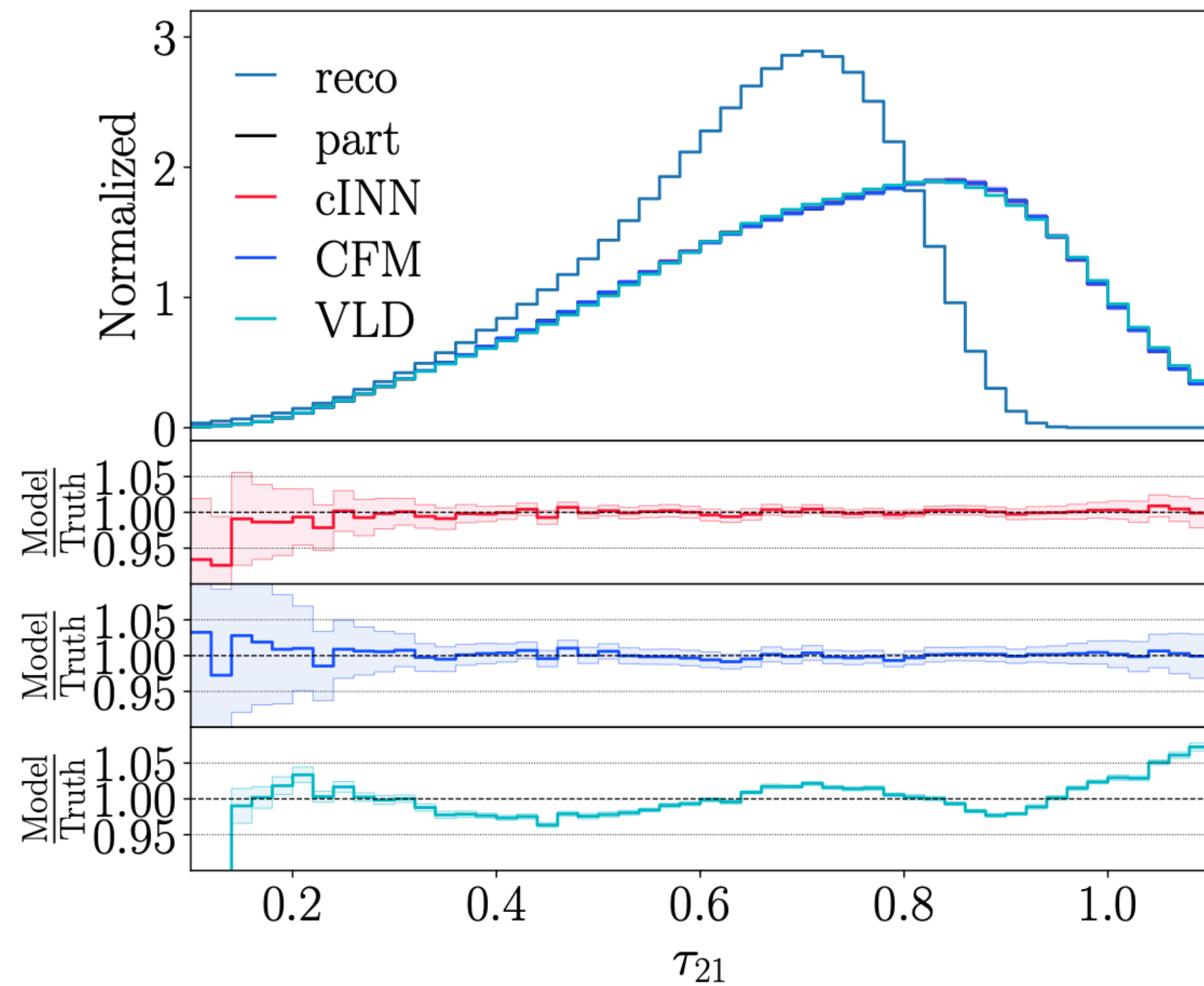
$$\frac{d}{dt}x(t) = v_\theta(x(t), t)$$

Diffusion Models

Unfolding

Unfolding with Diffusion

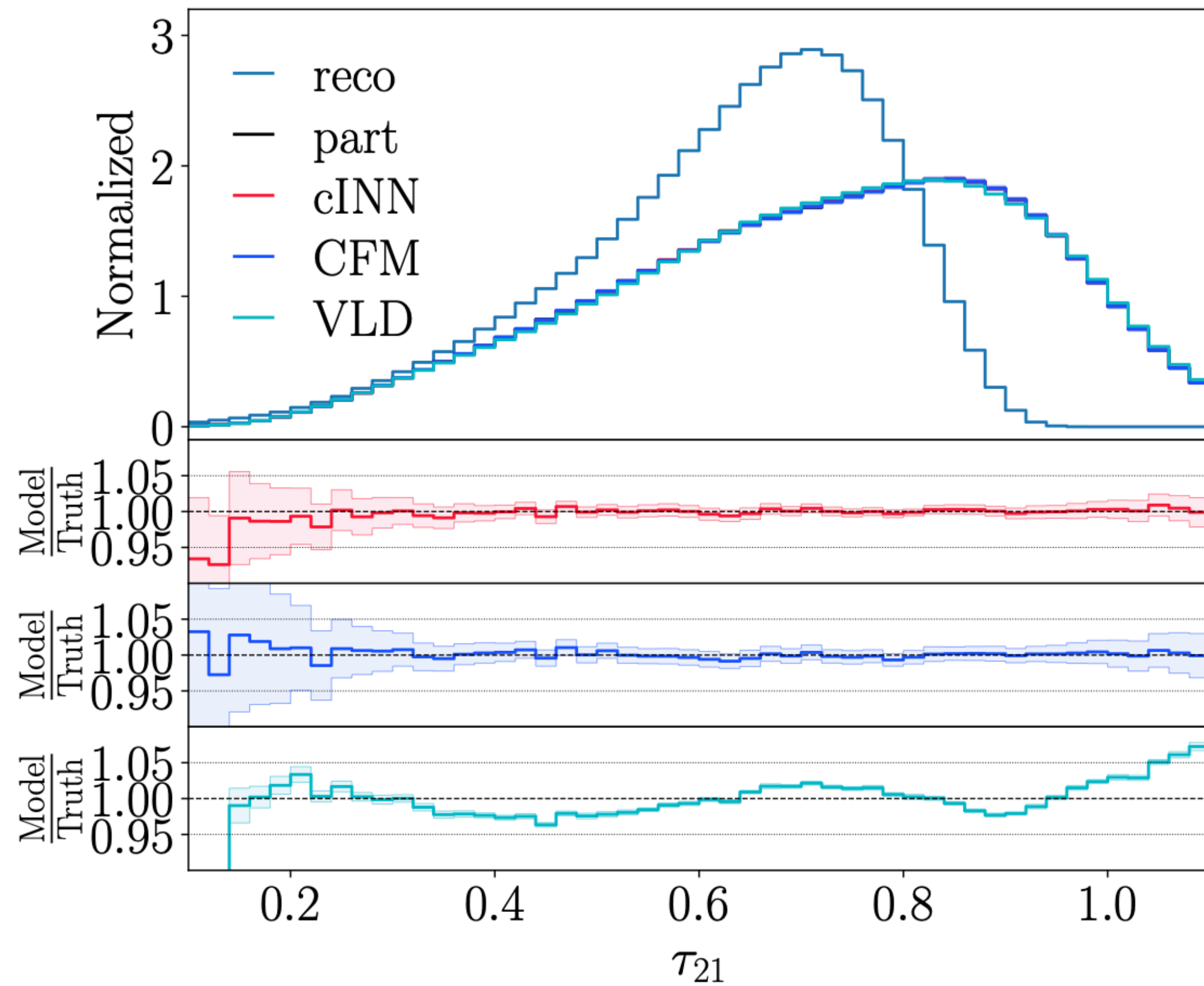
Z+jets (simple)



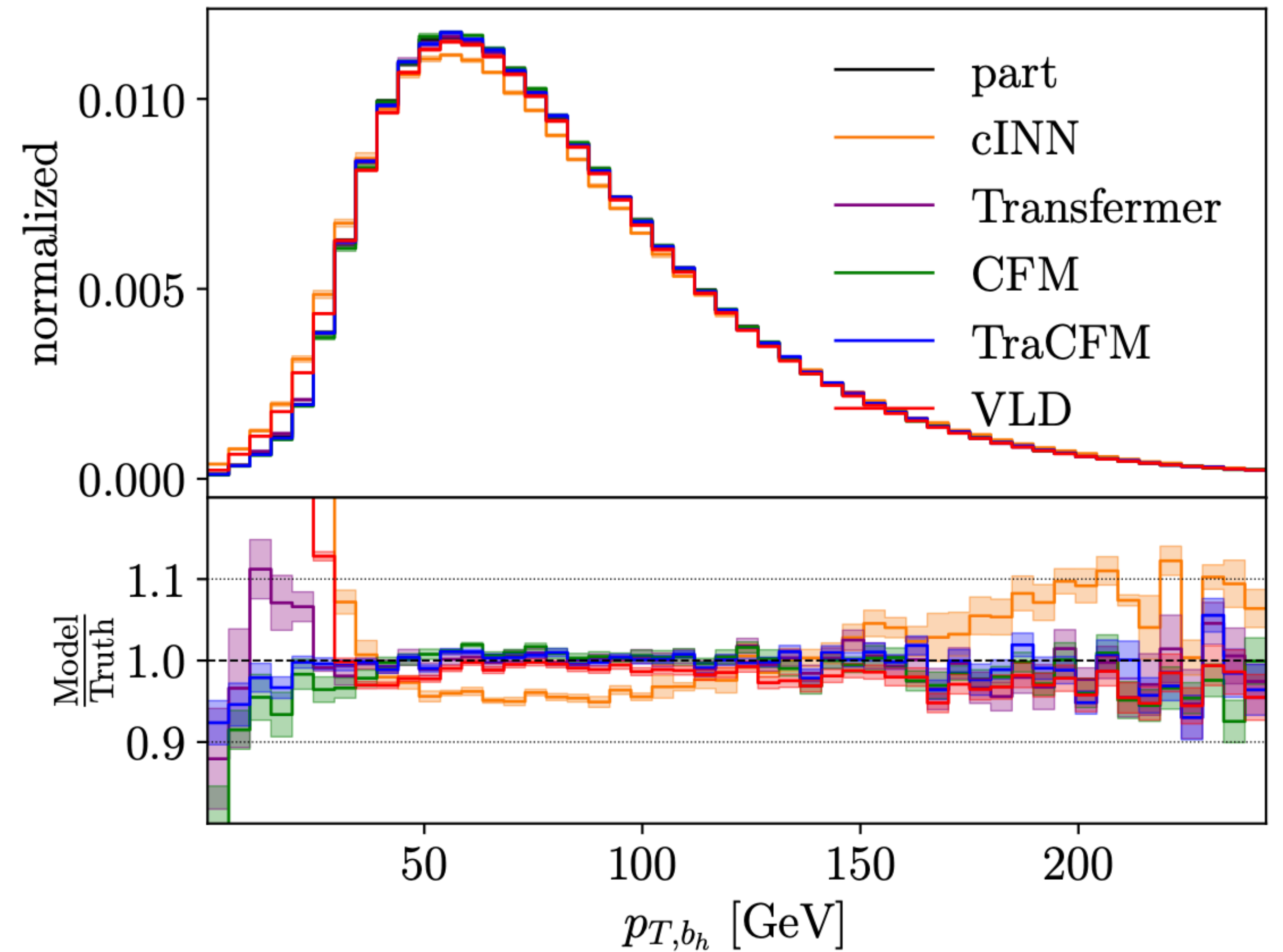
Unfolding with Diffusion

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Z+jets (simple)



Top-pair with decays (hard)





Open Discussion